

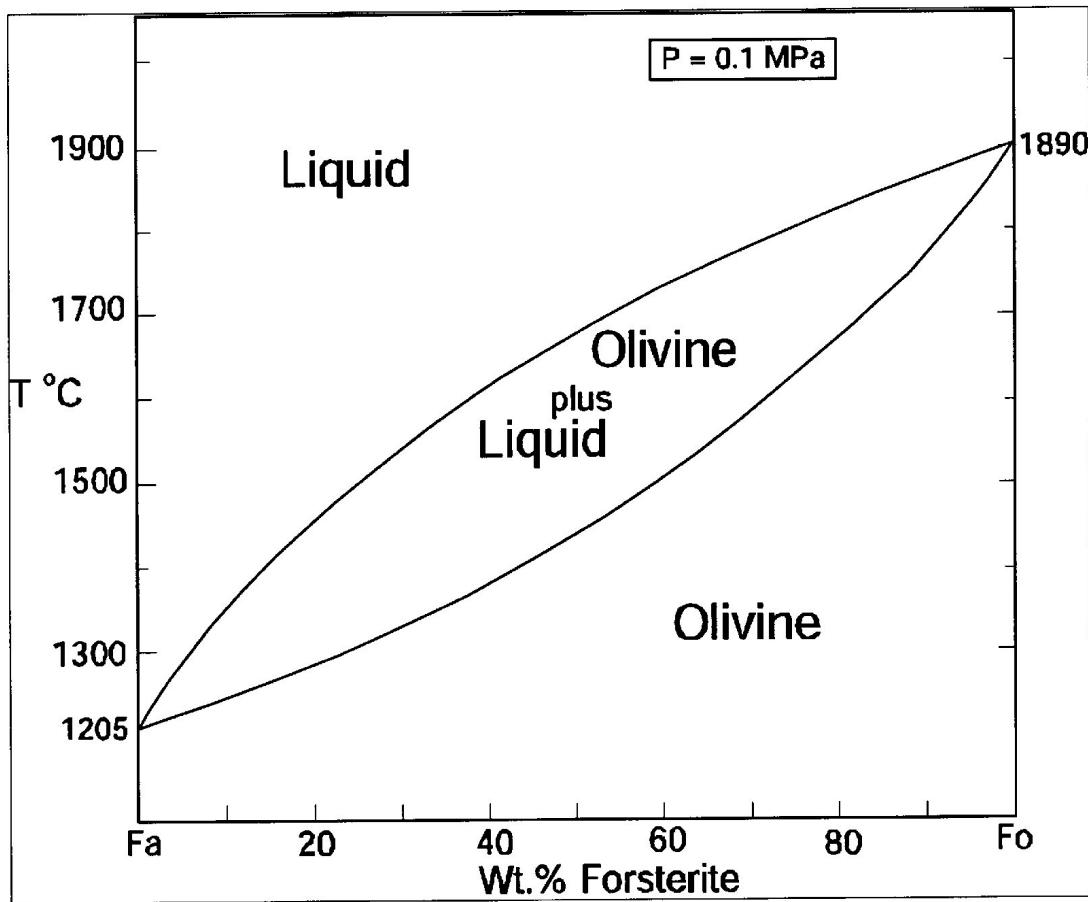
**The Phase Rule for isobaric or isothermal systems:**  $F = C - P + 1$

**P** = the number of phases: the number of different types of mechanically separable portions of the system (don't confuse this with pressure!)

**C** = components: the **minimum** number of chemical constituents that are required to define the composition of every phase in the diagram

**F** = variance or degrees of freedom: the number of intensive parameters that must be specified in order to completely determine the state of a system. Alternatively, F is the number of intensive parameters that can be changed independently without changing the parameters of the phase rule (i.e. losing or gaining a phase).

Consider the following system:



1. Does this graph describe an isobaric or isothermal system?

2. Find the point on the graph that represents the system  $\text{Fo}_{80}$  at  $1950^\circ\text{C}$  and label it point **A**. Determine **F** at point **A**.
3. What is/are the intensive parameter(s) described by **F**?
4. As composition **A** cools, at what temperature does **P** (# of phases) change?
5. This boundary you found in 4. is called the **liquidus**, because it describes the composition of the liquid at a given temperature. The line below it is called the **solidus**, because it describes the composition of the solid at the same temperature. The appearance of this graph is typical for a system with solid solution.  
Draw two horizontal lines across the graph at  $1700^\circ\text{C}$  and  $1800^\circ\text{C}$  and a vertical line from point **A** to the bottom of the graph. What is the composition of the melt at these two temperatures? What is the composition of the solid at these two temperatures?
6. Use the **lever rule** to determine the weight percent of the melt and the solid at  $1700^\circ\text{C}$  and  $1800^\circ\text{C}$ .

Here's how the **lever rule** works:

Assume our bulk system is at composition **A**, and at a particular temperature the composition of the liquid is represented by **X** and the composition of the solid is represented by **Y**.

**X**                    **A**                    **Y**

$$\begin{aligned}\text{Wt\% liquid} &= 100 \times \frac{AY}{XY} && \text{where } AY = \text{distance between A and Y, etc.} \\ \text{Wt\% solid} &= 100 \times \frac{XA}{XY}\end{aligned}$$

7. What is **F** when system **A** cools to  $1500^\circ\text{C}$ ? What is the composition of the solid? How does this compare to the initial composition of the melt?